



# Indraprastha College for Women

## University of Delhi

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| Course Name:       | B.A.(Prog.)        |
| Paper Title:       | Number Theory      |
| Unique Paper Code: |                    |
| Semester:          | V                  |
| Faculty(s):        | Dr. Gunjan Khurana |
| Year:              | 2024-2025          |

| <b>Work Plan</b>                          |          |  |   |
|---|----------|--|---|
| Period                                    | Unit No. | Learning Objective   | Topics to be Covered  |
| 1 <sup>st</sup> Aug -3 <sup>rd</sup> Aug  | 1        | The Euclidean algorithm and linear Diophantine equations, the Fundamental theorem of arithmetic and some of the open problems of number theory viz. the Goldbach conjecture. | The division algorithm, divisibility and the greatest common divisor                |
| 5 <sup>th</sup> Aug-10 <sup>th</sup> Aug  | 1        | Same as above  | Euclid's lemma; The Euclidean algorithm, Linear Diophantine equations               |
| 12 <sup>th</sup> Aug-17 <sup>th</sup> Aug | 1        | Same as above  | The Fundamental theorem of arithmetic, The sieve of Eratosthenes                    |
| 19 <sup>th</sup> Aug-24 <sup>th</sup> Aug | 1        | Same as above  | Euclid's theorem and the Goldbach conjecture; The Fibonacci sequence and its nature |
| 26 <sup>th</sup> Aug-31 <sup>st</sup> Aug | 2        | The modular arithmetic, linear congruence equations, system of linear congruence equations, arithmetic functions, and multiplicative functions, e.g., Euler's Phi-function.  | Congruence relation and its basic properties  |

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|---|----------------------|---|---|
| 2 <sup>nd</sup> Sep-7 <sup>th</sup> Sep   | 2                    | Same as above   | Linear congruences and the Chinese remainder theorem,                               |
| 9 <sup>th</sup> Sep-14 <sup>th</sup> Sep  | 2                    | Same as above   | System of linear congruences in two variables                                       |
| 16 <sup>th</sup> Sep-21 <sup>st</sup> Sep | 2                    | Same as above   | Fermat's little theorem and its generalization                                      |
| 23 <sup>rd</sup> Sep-28 <sup>th</sup> Sep | 2                    | Same as above   | Wilson's theorem and its converse   |
| 30 <sup>th</sup> Sep-5 <sup>th</sup> Oct  | 2                    | Same as above   | Number-theoretic functions for sum and the number of divisors of a positive integer |
| 7 <sup>th</sup> Oct-12 <sup>th</sup> Oct  | 2                    | Same as above   | Multiplicative functions  |
| 14 <sup>th</sup> Oct-19 <sup>th</sup> Oct | 2                    | Same as above   | The greatest integer function; Euler's phi-function and its properties              |
| 21 <sup>st</sup> Oct-26 <sup>th</sup> Oct | 3                    | Introduction of the simple encryption and decryption techniques, and the numbers of specific forms viz. Mersenne numbers, Fermat numbers etc. | Basics of cryptography, Hill's cipher   |
| 28 <sup>th</sup> Oct-2 <sup>nd</sup> Nov  | 3                    | Same as above   | MID SEMESTER BREAK  |
| 4 <sup>th</sup> Nov-9 <sup>th</sup> Nov   | 3                    | Same as above   | Public-key cryptosystems and RSA encryption and decryption technique                |
| 11 <sup>th</sup> Nov-16 <sup>th</sup> Nov | 3                    | Same as above   | Introduction to perfect numbers   |
| 18 <sup>th</sup> Nov-23 <sup>rd</sup> Nov | 3                    | Same as above   | Mersenne numbers and Fermat numbers   |
| 25 <sup>th</sup> Nov-27 <sup>th</sup> Nov |                      | Same as above   | Revision  |
| 28 <sup>th</sup> Nov                      | DISBERSAL OF CLASSES |   |   |
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| Unit | TOPICS  |
|------|---|
| I    | Divisibility and Prime Numbers (12 hours)<br>Revisiting: The division algorithm, divisibility and the greatest common divisor. Euclid's lemma; The Euclidean algorithm, Linear Diophantine equations; The Fundamental theorem of Arithmetic, The sieve of |

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|               | Eratosthenes, Euclid theorem and the Goldbach conjecture; The Fibonacci sequence and its nature.  |
| II            | Theory of Congruences and Number-Theoretic Functions (21 hours)<br>Congruence relation and its basic properties, Linear congruences and the Chinese remainder theorem, System of linear congruences in two variables; Fermat's little theorem and its generalization, Wilson's theorem and its converse; Number-theoretic functions for sum and the number of divisors of a positive integer, Multiplicative functions, The greatest integer function; Euler's Phi-function and its properties. |
| III           | Public Key Encryption and Numbers of Special Form (12 hours)<br>Basics of cryptography, Hill's cipher, Public-key cryptosystems and RSA encryption and decryption technique; Introduction to perfect numbers, Mersenne numbers and Fermat numbers.  |
| <b>S. No.</b> | <b>Name of Authors/Books/Publishers</b>   |
| 1.            | Burton, David M. (2011). Elementary Number Theory (7th ed.). McGraw-Hill Education Pvt. Ltd. Indian Reprint 2017.   |
| 2.            | Jones, G. A., & Jones, J. Mary. (2005). Elementary Number Theory. Undergraduate Mathematics Series (SUMS). Indian Reprint.  |
| 3.            | Robbins, Neville (2007). Beginning Number Theory (2nd ed.). Narosa Publishing House Pvt. Ltd. Delhi.  |
| 4.            | Rosen, Kenneth H. (2011). Elementary Number Theory and its Applications (6th ed.). Pearson Education. Indian Reprint 2015.  |